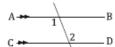
## Period: Name: Logic Problems with Parallel Lines Cut by Transversals

Geometry

Okay, these problems are very popular with teachers and test writers because they are supposed to be harder. They are really not if you can remember a few simple things. I'll go over what these things are, then we will practice using them on logic problems. You will no longer lose precious minutes of sleep over them. Let's go!

First, for alternate interior angles, corresponding angles, and alternate interior angles, the lines MUST BE PARALLEL if they are equal in measure. They must also be parallel for consecutive angles to add to 180°. Here are a couple of pictures to illustrate this point.



In this figure ∠1 and ∠2 are alternate interior and because AB and CD are parallel,  $m \angle 1 = m \angle 2$ .

In this fig ∠1 and ∠2 are alternate interior. BUT, because AB and CD are NOT parallel,  $m \angle 1 \neq m \angle 2$ .

This goes for any of the above kinds of angles. Remember consecutive angles add to 180° if the lines are parallel.

Second, and this is the weirder one, you can find out if the lines are parallel by seeing if alternate interior angles, corresponding angles, or alternate exterior angles are equal in measure. Or, if consecutive angles add to 180°. If ANY of these is true, then the lines are certainly parallel. This idea is called the converse of the first point (no not the shoes). We will talk about this fine footwear in a later section. Let's look at a few examples of this.

Ex. 1. In the figure below, m∠1=m∠2. Is AB||CD? Ex. 2. Must AB||CD? Explain: Explain.



and ∠2 are corresponding, the lines are parallel. This is because in order for m∠1 to equal m∠2 the lines must be parallel in the first place! (the first idea)

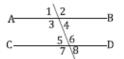
Answer: YES! Why? Because m∠1=m∠2 and ∠1 Answer: NO! Why? Because we don't know if m∠1=m∠2 even though ∠1 and ∠2 are alternate exterior, the lines don't have to be parallel, (I suppose they could be, but we don't know FOR SURE,)

Notice that in these examples the lines look parallel. Remember, looks can be deceiving. You have to go by what the question is telling you. Don't ever say, "well it looks like it." That usually gets you into trouble in Geometry.

Thirdly, vertical angles and linear pairs are not effected by whether or not the lines are parallel, and you can't say the lines are parallel if you have either of these two. So why mention it? Because they are often used as distractors (multiple choice answers that are wrong) for these kinds of problems. Let me show you what I mean.

Page 1 front

Period: Name: Ex. 3. In the figure below which pair of angles must be equal to show ABIICD? Explain.



A. 1 and 4

B. 5 and 6

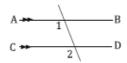
C. 7 and 3

D. 7 and 6

Answer: C! Why? Because A is a pair of vertical angles. If these are equal who knows if AB||CD. Same with choice D. Choice B names a linear pair which will add to 180° whether the lines are parallel or not. So, that leaves C, a pair of corresponding angles. A, B and D are distractors.

For these\_read each question. Mark "T" for True and "F" for False, and then explain your answer.

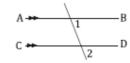
m∠1 = m∠2?



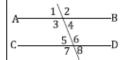
m∠1 = m∠2?



5. m∠1 =m∠2?



Ex. 4. In the figure below, which pair of must be equal to show AB||CD? Explain.



A. 1 and 7

B. 5 and 6

C. 7 and 6

D. 5 and 4

Answer: D! Why? Because A is actually a pair of supplementary angles (m7=m3 and m3+m1=180°, so m1+m7=180°). B is another linear pair, and C is a pair of vertical angles. This leaves us with choice D.

Okay, now you try some for real...

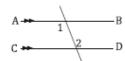
m∠1 =m∠2?



4. m∠1 =m∠2?



6 m∠1 =m∠2?



Page 1 back side

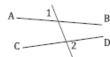
ubble T for True and F for False.									
#1.	#2.	#3.	#4.	#5.	#6.				
OT	OT	ΟT	ΟT	OT	ΟT				
○ F	OF	OF	OF	○ F	OF				

## 2.1.5

# Period: Name: Which two angles must have the same measure to show that AB|| CD?

#### Period: Name:

m∠1 =m∠2?



3. m∠1+m∠2=180°?



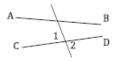
5. m∠1=m∠2 is AB||CD?



m∠1=m∠2 is AB||CD?



m∠1 =m∠2?



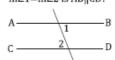
4. m∠1+m∠2=180°?

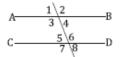


m∠1=m∠2 is AB||CD?

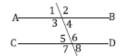


m∠1=m∠2 is AB||CD?

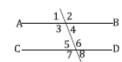




- A. 3 and 2
- B. 5 and 4
- C. 7 and 6
- D. 5 and 6
- 3. Which two angles must have the same measure to show that AB|| CD?

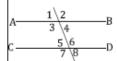


- A. 2 and 5
- B. 7 and 6
- C. 6 and 8
- D. 8 and 1
- 5. Which two angles must have the same measure to show that AB|| CD?

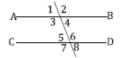


- A. 1 and 3
- B. 7 and 2
- C. 1 and 4
- D. 2 and 8

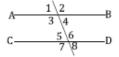
Geometry Nong
Which two angles must have the same measure to show that AB|| CD?



- A. 1 and 5
- B. 1 and 4
- C. 3 and 4
- D. 3 and 8
- Which two angles must have the same measure to show that AB|| CD?



- A. 6 and 2
- B. 5 and 6
- C. 7 and 8
- D. 5 and 8
- Which two angles must have the same measure to show that AB|| CD?



- A. 5 and 8
- B. 5 and 7
- C. 4 and 8
- D. 1 and 2
- Page 2 back side

### Page 2 Front

							•	
Bubble T for	True and F f	or False.						
#1.	#2.	#3.	#4.	#5.	#6.	#7.	#8.	I
OT	OT	OT	OT	OT	OT	OT	OT	l
OF	OF	OF	OF	OF	OF	OF	OF	l

Bubble the correct answer choice from each item above.

#1.	#2.	#3.	#4.	#5.	#6.
O A.	OA.	O A.	OA.	O A.	OA.
○ B.	○B.	○ B.	○B.	○ B.	OB.
O C.	OG.	O C.	OC.	OC.	OC.
O D.	OD.	○ D.	○D.	○ D.	OD.

## Period: Name: Angles Formed From Parallel Lines Cut by a Transversal

Geometry

Yes, that is a mouthful, and so is each member of this next set of angles, but with a little practice and a little persistence it's easy!

First, what the heck are Parallel Lines Cut by a Transversal? Well let's see,



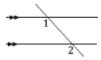
See how the parallel lines are both going the same direction? The Transversal is just an unnecessarily fancy name for that lines that intersects both of the parallel lines.

Now let's look at this...



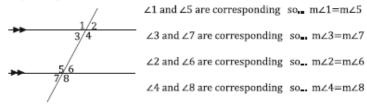
See the difference in this figure? The lines are not parallel. That's okay, all of these angles still have the same name. If the lines aren't parallel none of them are equal. Confused? As Yoda would say, "You will be." Ah, but who cares, he's just a silly green guy who lives in a swamp and has grammar problems. It's really not that bad. Let's look at the first pair of angles already....

Corresponding Angles (memorize me)



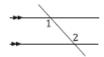
Corresponding Angle Theorem: If two parallel lines are cut by a transversal then corresponding angles are congruent and equal in measure.

If the lines aren't parallel they aren't equal; that's not so bad, huh? In your face, Yoda! No! Put me down! I didn't mean it! Okay seriously, corresponding angles are always on the same side of the transversal as each other, and on the same side of their respective parallel lines. That is how you remember them. In the previous example ∠1 is below and to the left and so is ∠2 so they are corresponding. Here are all of them.



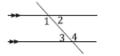
Alternate Interior Angles (memorize me)





Alternate Interior Angle Theorem: If two parallel lines are cut by a transversal then alternate interior angles are equal in measure.

Again, if the lines aren't parallel these are not equal. Alternate means opposite. Like the alternate side of the street from where you live. To get there go across the street! Interior means inside, (How often do you see an interior decorator hanging curtains on the outside of a house? Not a good idea trust me.) So, alternate interior means "opposite inside". Opposite, as in on opposite sides of the transversal, and inside, as in inside the parallel lines. You have to kind of stare at them a while to see what I mean, but when you see it you won't forget it. So stare away! (I'm not joking about the staring. It actually helps to stare at them until you get used to where they are.)



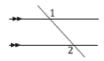
∠1 and ∠4 are alternate interior so.. m∠1=m∠4

∠2 and ∠3 are alternate interior so m∠2=m∠3

Also note that there are only two pairs of these things in the picture, so they are pretty easy to find.

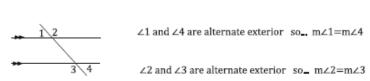
Alternate Exterior Angles (memorize me)

Can you guess where these are just by the name?



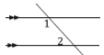
Alternate Exterior Angle Theorem: If two parallel lines are cut by a transversal, then alternate exterior angles are equal in measure.

Yup, you guessed it. Exterior means outside, so these are "opposite outside" angles, as you can see if you stare again for a while\_



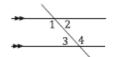


# 2.1.5 **P2** of 4



Consecutive Angle Theorem: If two parallel lines are cut by a transversal then the sum of the measures of consecutive angles is 180°.

Again, if the lines aren't parallel this isn't true either. This one is a bit different. These are on the same side of the transversal and on the inside of the parallel lines. They are different because they add to 180°. That is because in the following picture ∠2 is actually corresponding to angle ∠3 and therefore equal. You already know ∠2 and ∠3 are a linear pair (or at least you should). So then it follows that ∠1 and angle ∠2 also add to 180°. Now begin the staring!

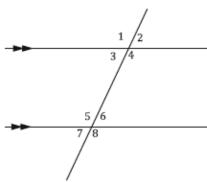


∠1 and ∠3 are consecutive so\_ m∠1+m∠3=180°

∠2 and ∠4 are consecutive so\_ m∠2+m∠4=180°

Great! So now we have corresponding, alternate interior, alternate exterior and consecutive angles. We will do a few exercises to help you memorize them. But .. if you don't have a clue what they are go back and read and stare for a while longer until you do. Hey, I told you I would tell you the best way to learn this. If there was another way besides staring I would tell you. It's like you have to memorize these positions visually. For example, you can stare at a picture of your favorite person and then close your eyes and picture their face, right? It's the same thing with these angles. If you can close your eyes and picture where they all are then you're ready,

For your first set of problems, list all of the pairs of each type of angle. Refer to the instructions if yo need to. (Don't feel bad about looking back, Everyone will need to on these first few problems.)



1. List all the pairs of corresponding angles:

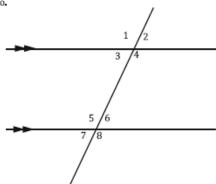
2. List all the pairs of alternate interior angles:

List all the pairs of alternate exterior angles:

4. List all the pairs of consecutive angles:

Easy as an abelian ring!!!! Let's do some more... © 2010 www.letspracticegeometry.com

For our first exercise, bubble the correct answer choice for each item below. Refer to the previous pages if you need to.



∠1 and ∠5 are.

A. Corresponding

B. Alternate Interior

C. Alternate Exterior

D. Consecutive

∠3 and ∠6 are\_

A. Corresponding

B. Alternate Interior

C. Alternate Exterior

D. Consecutive

∠4 and ∠5 are...

A. Corresponding

B. Alternate Interior

C. Alternate Exterior

D. Consecutive

10. ∠4 and ∠8 are...

A. Corresponding

B. Alternate Interior

C. Alternate Exterior

D. Consecutive

2. ∠8 and ∠4 are...

B. Alternate Interior

C. Alternate Exterior

D. Consecutive

∠6 and ∠4 are...

A. Corresponding

B. Alternate Interior

C. Alternate Exterior

D. Consecutive

8. ∠1 and ∠8 are...

A. Corresponding

B. Alternate Interior

C. Alternate Exterior

D. Consecutive

∠2 and ∠7 are.

A. Corresponding A. Corresponding

B. Alternate Interior

C. Alternate Exterior

D. Consecutive

∠2 and ∠6 are...

A. Corresponding

B. Alternate Interior

C. Alternate Exterior

D. Consecutive

∠3 and ∠5 are...

A. Corresponding

B. Alternate Interior

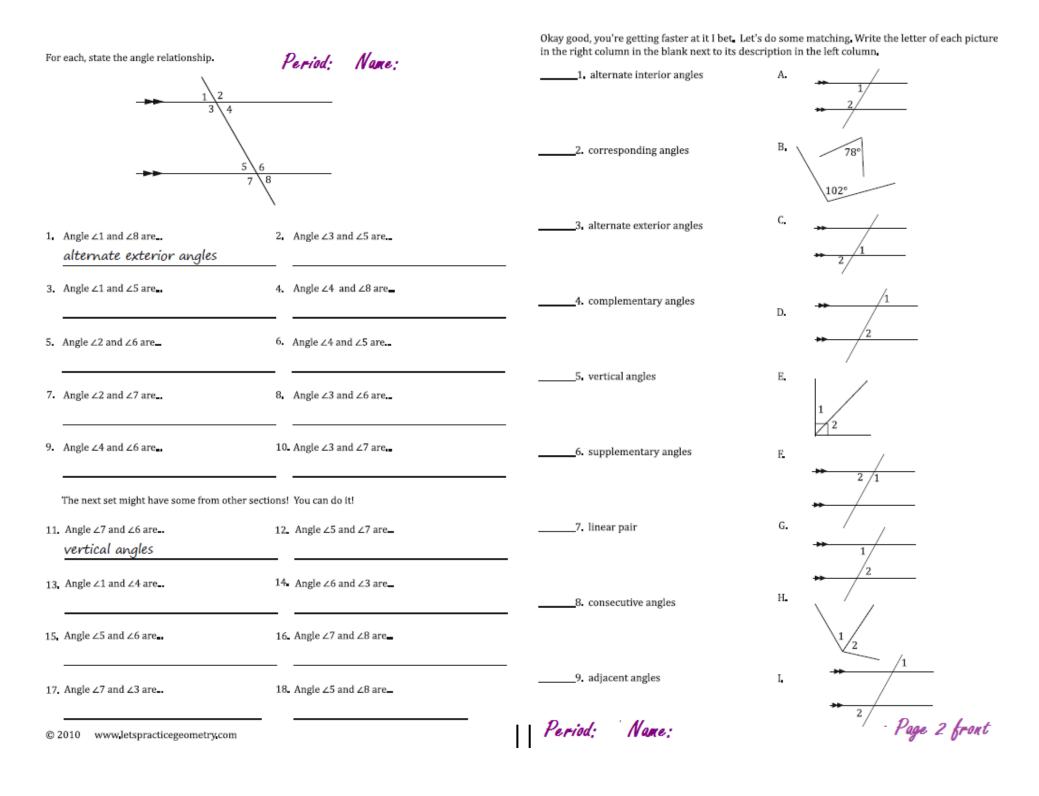
C. Alternate Exterior

D. Consecutive

Great Job, these are tough to remember which is which. If you are struggling, go back and try to memorize what each one looks like. (like remembering a picture) If you do that these will become very easy. Let's do some more!

Page 1 back side

Bubble the correct answer choice from each item above.										
#1.	#2.	#3.	#4_	#5.	#6.	#7.	#8.	#9.	#10.	
ΟA.	OA.	OA.	OA.	OA.	OA.	OA.	OA <b>.</b>	OA.	OA.	
OB.	OB•	OB.	OB.	OB.	OB.	OB.	OB.	OB•	OB.	
OC.	OG.	OG.	OC.	OG.	OC.	OC.	OC.	OC.	OG.	
OD.	OD.	OD.	OD.	OD.	OD.	#7. OB. OC. OD.	○D.	OD.	OD.	



Let's take it up a notch\_for each, write the angle 2. relationship you see in the picture and a statement of whether the angles are equal or add to 180°.

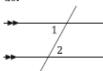


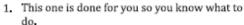
On these state the angle relationship, write a statement about whether they add to  $180^{\circ}$  or are equal, and solve for x if necessary.

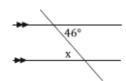
2.1.5

**P2** of 4

 This one is done for you so you know what to do.

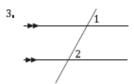




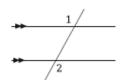




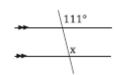
#### Alternate interior, m21=m22



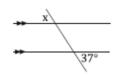
6.



3.

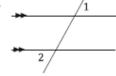


4

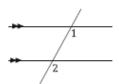


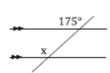
68°

5.



7.





5.



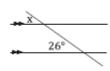
8.



9



7.



Great job!!

Period: Name:

Period: Name:

Page 2 back side

Bubble all the correct answers from above, Don't bubble incorrect answers,



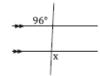




12.



#### 14.

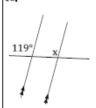




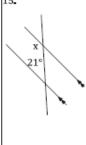
11.



13.



15.



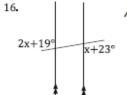
Bubble all the correct answers from above. Don't bubble incorrect answers.

 $\bigcirc 31^{\circ} \ \bigcirc 132^{\circ} \ \bigcirc 54^{\circ} \ \bigcirc 96^{\circ} \ \bigcirc 159^{\circ} \ \bigcirc 122^{\circ} \ \bigcirc 83^{\circ} \ \bigcirc 119^{\circ} \ \bigcirc 154^{\circ} \ \bigcirc 113^{\circ} \ \bigcirc 67^{\circ} \ \bigcirc 52^{\circ} \ \bigcirc 58^{\circ} \ \bigcirc 126^{\circ}$ 

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On these state the angle relationship, write a statement about whether they add to 180° or are

equal, and find the value of x. Alternate exterior



x+34°

2x-12

18.

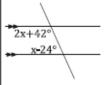
20.

3x + 21

17.

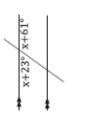
2.1.5 **P2** of 4

19.

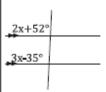


2x-61°

21.



22.



Name: Period:

Page 3 front

Bubble all the correct answers from above. Don't bubble incorrect answers.

### 2.1.5

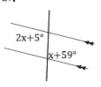
23.



25.



27.



29.



**P2** of 4

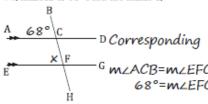


26. 3x+71° 5x+37

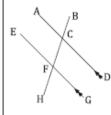
30.

Mark the diagram with the given information, state the angle relationship, and then solve for the indicated angle.

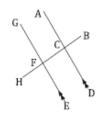
31. m∠ACB is 68° Find the m∠EFC.



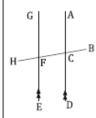
32, m∠DCH=85° Find m∠BFE.



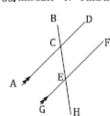
33, m∠EFB=91° Find m∠DCH.



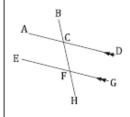
34. m∠HFG=103° Find m∠BCD.



35. m∠GEH=47° Find m∠BEF.



36. m∠DCH=63° Find m∠ACH.



Bubble all the correct answers from above. Don't bubble incorrect answers.

 $\bigcirc 31^{\circ} \ \bigcirc 116^{\circ} \ \bigcirc 20^{\circ} \ \bigcirc 17^{\circ} \ \bigcirc 54^{\circ} \ \bigcirc 98^{\circ} \ \bigcirc 51.5^{\circ} \ \bigcirc 45^{\circ} \ \bigcirc 60^{\circ} \ \bigcirc 72.5^{\circ} \ \bigcirc 65^{\circ} \ \bigcirc 44^{\circ} \ \bigcirc 30.5^{\circ} \ \bigcirc 24^{\circ}$ 

Period: Name:

Bubble all the correct answers from above. Don't bubble incorrect answers.

○112° ○95°











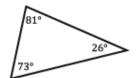




# Triangle Sum Theorem Period: Name:

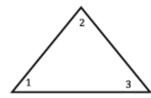
AKA: the triangle interior angle sum theorem (I know that doesn't help).

The <u>Triangle Sum Theorem</u> is really, really easy to explain. If you add all the interior (inside) angles of any triangle they always add to 180°. Why? Why do they ask for your phone number when you buy batteries at Radio Shack? I don't know; they just do. It goes like this.



81°+26°+73°=180°

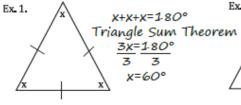
And like this\_



m∠1+m∠2+m∠3=180°

A couple of reminders from our section on the basics. An equilateral triangle has 3 equal angles. So.  $180^{\circ}/3=60^{\circ}$ . Every angle in an equilateral triangle is  $60^{\circ}$ . They are also all the same. Look at these two examples.

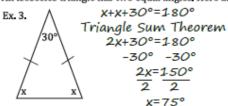
Solve for x.

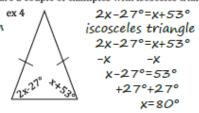


2x-12=60° equilateral triangle 2x-12=60° +12 +12° 2x=72° 2 2

x=36°

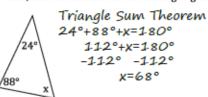
An isosceles triangle has two equal angles. Here are a couple of examples with isosceles triangles.

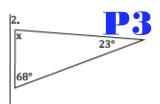


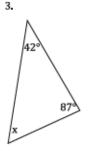


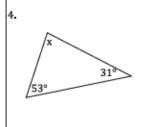
Let's do a bunch of problems to turn you into a Trianlge Sum Theorem expert.

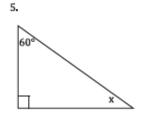
For each, find the measure of the missing angle.

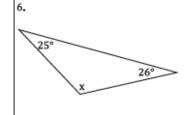


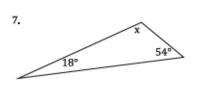


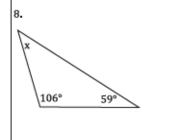






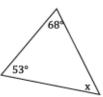


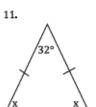


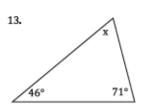


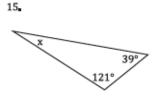
Page 1 front

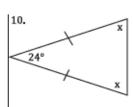
Bubble all the correct answers from above. Don't bubble incorrect answers.

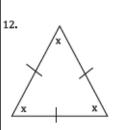


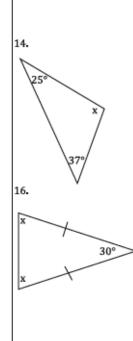






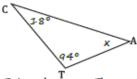






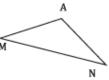
Mark the diagram with the given information. Then, find the measure of the indicated angle.

17. m∠C=18°, m∠T=94°. Find m∠A.

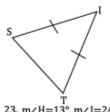


Triangle Sum Theorem 18°+94°+x=180° 112°+x=180° -112° -112° x=68° mZA=68°

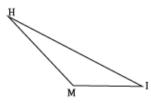
19. m∠A=138°, m∠N=17°. Find m∠M.

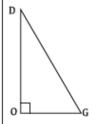


21. m∠I=48°, Find m∠T,

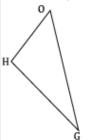


23. m∠H=13°, m∠I=24°. Find m∠M.

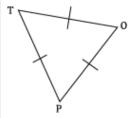




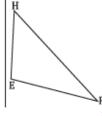
m∠0=47°, m∠G=43°. Find m∠H.



Find m∠0, m∠T, and m∠P.



24. m∠E=118°, m∠R=26°. Find m∠H.



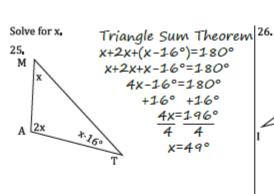
#### Period: Name:

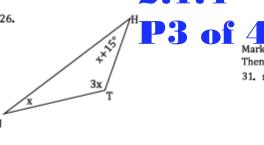
Page 1 back side

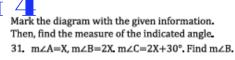
Bubble all the correct answers from above. Don't bubble incorrect answers.

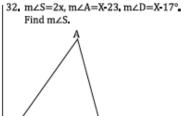
Bubble all the correct answers from above. Don't bubble incorrect answers.

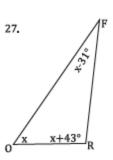
# 2.1.4

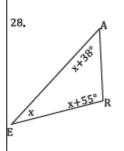


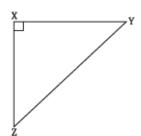






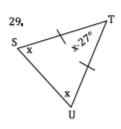


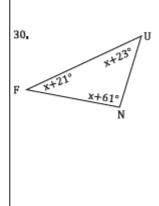




m∠Y=x+5°, m∠Z=x-7°. Find m∠Z.

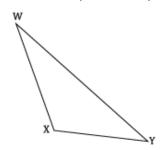
34. Find m∠R, m∠Q, and m∠S.







35. m W=x-22°, m X=3x+19°, m Y=x-17°. Find m X.



Page 2

#### Períod: Name:

Bubble all the correct answers from above. Don't bubble incorrect answers.

○165° ○25° ○69° ○27° ○29° ○55° ○56° ○39° ○33° ○49

Bubble all the correct answers from above. Don't bubble incorrect answers.

 $\bigcirc 39^{\circ} \quad \bigcirc 60^{\circ} \quad \bigcirc 139^{\circ} \quad \bigcirc 60^{\circ} \quad \bigcirc 110^{\circ} \quad \bigcirc 55^{\circ} \quad \bigcirc 50^{\circ} \quad \bigcirc 46^{\circ} \quad \bigcirc 31^{\circ} \quad \bigcirc 92^{\circ} \quad \bigcirc 40^{\circ}$  © 2010 www.letspracticegeometry.com

# Geometry 4

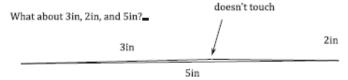
#### Triangle Inequality Theorem

How not to make a triangle...

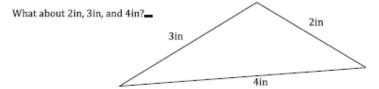
The Triangle Inequality Theorem is used to answer a simple kind of question— can you make a triangle with side lengths of 2in, 3in, and 6in? Let's see—



Does that look like a triangle? No! Why? Because it's not closed. Now I suppose you could slide the 2in and 3in sides closer together, but then the third wouldn't be 6in anymore. There is just no way to do it! Notice that 3+2=5 and 5<6.



Nope... notice that little gap I pointed out for you? This doesn't work either.. In fact if you made the 2in and 3in touch by swinging them just a little closer to the 5in side they would touch. In fact, they would make a straight line. No triangle here. Notice that 2+3=5 and 5=5.



Ah! Now that's a triangle if I ever saw one\_Notice that 2+3=5 and 5>4. So the <u>Triangle Inequality Theorem</u> goes like this... For any triangle the sum of the lengths of any two sides must be greater than the length of the third side. That is s1+s2>s3. If this is not true then sorry, no triangle.

Try this... Do the lengths 18, 15, and 27 make a triangle?

s1+s2=s3 18+15>27 33>27 True! So... yes they do!

What about 87,91 and 456?

s1+s2=s3 87+91>456 178>456 False! No triangle here!

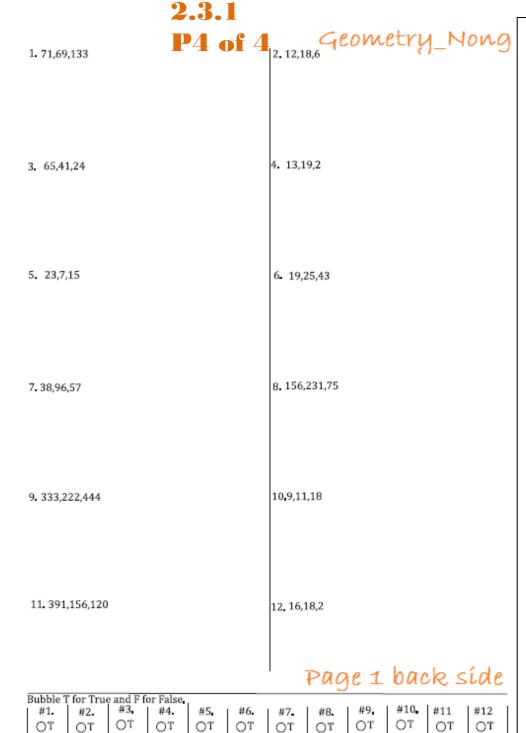
Let's practice!

If the three numbers could be the sides of a 2.7,7,13 triangle, bubble "T." If not, bubble "F." Make sure to show your work. 1. 4.7,11 51+52=53 4+7>1.1 11>11 false! no triangle 4. 6,10,12 3, 4,3,6 6-34,18,21 5. 9,2,5 (You might have to put some of these in 51+52=53 2+5>9 7>9 False! no triangle 8, 45,91,46 7.8,17,9 10, 36, 25, 61 9. 48,52,80 11,128,86,76 12, 25, 70, 48

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Bubble I	for True	and F fe	or False									
#1.	#2.	#3.	#4.	#5	#6.	#7.	#8.	#9.	#10.	#11	#12	
$\cap$ T	$\bigcirc$ T	OT	OT	$\bigcirc$ T	OT	OT	OT	OT	OT	OT	$\bigcirc$ T	
●F	OF	OF	#4. OT	OF	○F	OF	OF	○F	OF	OF	○F	



OF.

OF.

OF.

#### **Geometry student directions:**

- 1. Copy each question and solve it in your notebook. Date & Title it with the NAME on each stabled packet. This is kept in your notebook (notes).
- 2. Grading this work: there are Google forms to be submitted to Ms. Nong posted.

After you hit SUBMIT: Do write your score in your notebook and corrected answers.

When you still don't get how to get the correct answers you must ask!

#### WHY?

--Eliminate paper work(s)
--Hybrid/online learning & update your 21<sup>st</sup>
century skills

... more? [your turn to come up with more answers]